



http://www.bomsr.com

Email:editorbomsr@gmail.com

RESEARCH ARTICLE

A Peer Reviewed International Research Journal



**ON PRE GENERALIZED PRE REGULAR WEAKLY CONTINUOUS MAPS IN
TOPOLOGICAL SPACES**

R.S.WALI¹ AND VIVEKANANDA DEMBRE²

¹Department of Mathematics, Bhandari and Rathi College Guledagudd, Karnataka, India.

²Department of Mathematics, Rani Channamma University, Belagavi, Karnataka, India.



R.S.WALI

ABSTRACT

In this paper, a new class of maps called Pgprw-Continuous maps are introduced and investigated. A map $f: X \rightarrow Y$ is called pgprw-continuous maps if the inverse image of every closed set in Y is pgprw closed set in X and some of their properties are studied.

Key words: Pgprw closed sets, Pgprw open sets, Pgprw- continuous maps.

AMS Mathematical Subject classification(2010):54A05,54C05,54C08.

©KY PUBLICATIONS

1.INTRODUCTION

The Concept of semi-continuous maps was introduced and studied by Levine [1], Mishra et.al[2], Benchalli and Wali[3], Abd El-Monsef, El-deeb and Mahmoud[4], Jayalakshmi and Janaki[5], Vadivel and Vairamanickam[6], Joshi, Gupta, Bharadwaj Kumar and Kumar[7], Bhattacharya[8], Janaki and Renu Thomas[9], Shlya Isac Mary and Thangvely[10], Mashhour, Abd El-Monsef, El-deeb & El-deeb [11], Maki, Umehara and Noiri [12], Navalagi, Chandrashakarappa and Gurushatanavar [13], Gnanambal [14], Bhattacharya and Lahiri [15], Arya and Gupta [16] introduced and studied rgw-continuous maps, rw-continuous maps, β -continuous maps, $wg\alpha$ -continuous, $r\alpha$ -continuous maps, gprw-continuous maps, gr-continuous maps, R^* -continuous maps, rps-continuous maps, p-continuous maps, gp-continuous maps, gspr-continuous maps, gpr-continuous maps, sg-continuous maps, completely continuous maps respectively. In this paper, a new class of maps called pgprw continuous maps are introduced and investigated.

2.PRELIMINARIES

Throughout this paper space $(X, \tau), (Y, \sigma) \& (Z, \mu)$ (or simply $X, Y \& Z$) always denote topological space on which no separation axioms are assumed unless explicitly stated. For a subset A of a space X , $Cl(A)$, $Int(A)$, A^c , $P-Cl(A)$ and $P-int(A)$ denote the Closure of A , Interior of A , Compliment of A , pre-closure of A and pre-interior of (A) in X respectively.

Definition 2.1:[6] A subset A of topological space (X, τ) is called a $rg\alpha$ -closed set if $\alpha-Cl(A) \subseteq U$, Whenever $A \subseteq U$ and U is regular α - open in X .

Definition 2.2:[17] A subset A of topological space (X, τ) is called a pre generalized pre regular weakly closed set (briefly pgprw-closed set) if $pCl(A) \subseteq U$ whenever $A \subseteq U$ and U is $rg\alpha$ -open in (X, τ) .

Theorem 2.3:[17] If a subset A of (X, τ) is pre-closed set, then it is pre generalized pre regular weakly closed set but not conversely.

Theorem 2.4:[17] If a subset A of (X, τ) is closed, then it is pgprw-closed but not conversely.

Theorem 2.5:[17] If a subset A of (X, τ) is pgprw closed set, then it is gpr-closed set but not conversely.

Theorem 2.6:[17] If a subset A of (X, τ) is pgprw closed set, then it is gspr-closed set but not conversely.

Theorem 2.7:[17] If a subset A of (X, τ) is pgprw closed set, then it is gp closed set but not conversely.

Theorem 2.8:[18] If a subset A of (X, τ) is called pre generalized pre regular weakly open set if A^c is a pgprw closed.

Theorem 2.9:[19] Let A be a subset of (X, τ) Then $pgprw-cl(A)$ of A is defined to be the intersection of all pgprw-closed sets containing A and is denoted by $pgprw-cl(A)$.

Definition 2.10:[20] A subset A of topological space (X, τ) is called Regular open set if $A = int(cl(A))$ and a regular closed set if $A = cl(int(A))$.

Definition 2.11: A map $f: (X, \tau) \rightarrow (Y, \sigma)$ is said to be

(i) Completely continuous map [16] if $f^{-1}(V)$ is a regular closed set of (X, τ) for every closed set V of (Y, σ) .

(ii) semi-continuous map [1] if $f^{-1}(V)$ is a semi-closed set of (X, τ) for every closed set V of (Y, σ) .

(iii) Rgw-continuous map [2] if $f^{-1}(V)$ is a rgw-closed set of (X, τ) for every closed set V of (Y, σ) .

(iv) Rw-continuous map [3] if $f^{-1}(V)$ is a rw-closed set of (X, τ) for every closed set V of (Y, σ) .

(v) β -continuous map [4] if $f^{-1}(V)$ is a β -closed set of (X, τ) for every closed set V of (Y, σ) .

(vi) $wg\alpha$ -continuous map [5] if $f^{-1}(V)$ is a $wg\alpha$ -closed set of (X, τ) for every closed set V of (Y, σ) .

(vii) $Rg\alpha$ -continuous map [6] if $f^{-1}(V)$ is a $Rg\alpha$ -closed set of (X, τ) for every closed set V of (Y, σ) .

(viii) gprw continuous map [7] if $f^{-1}(V)$ is a gprw-closed set of (X, τ) for every closed set V of (Y, σ) .

(ix) gr continuous map [8] if $f^{-1}(V)$ is a gr closed set of (X, τ) for every closed set V of (Y, σ) .

(x) R^* continuous map [9] if $f^{-1}(V)$ is a R^* -closed set of (X, τ) for every closed set V of (Y, σ) .

(xi) Rps continuous map [10] if $f^{-1}(V)$ is a rps-closed set of (X, τ) for every closed set V of (Y, σ) .

(xii) p-continuous map [11] if $f^{-1}(V)$ is a p-closed set of (X, τ) for every closed set V of (Y, σ) .

(xiii) gp-continuous map [12] if $f^{-1}(V)$ is a gp closed set of (X, τ) for every closed set V of (Y, σ) .

(xiv) gspr-continuous map [13] if $f^{-1}(V)$ is a gspr closed set of (X, τ) for every closed set V of (Y, σ) .

(xv) gpr-continuous map [14] if $f^{-1}(V)$ is a gpr-closed set of (X, τ) for every closed set V of (Y, σ) .

(xvi) sg-continuous map [15] if $f^{-1}(V)$ is a sg closed set of (X, τ) for every closed set V of (Y, σ) .

3. PGPRW-CONTINUOUS MAPS AND THEIR BASIC PROPERTIES

Definition 3.1: A map $f: (X, \tau) \rightarrow (Y, \sigma)$ is said to be pgprw continuous maps (briefly pgprw-continuous) if the inverse image of every closed set in Y is pgprw closed set in X .

Theorem 3.2: If a map $f: (X, \tau) \rightarrow (Y, \sigma)$ is continuous map then it is pgprw-continuous map, but not conversely.

Proof: It is clearly by theorem [2.4].

Example 3.3: Let, $X=Y=\{a,b,c,d\}$, $\tau=\{X, \emptyset, \{a\}, \{b\}, \{a,b\}, \{a,b,c\}\}$ and

$\sigma = \{Y, \emptyset, \{a\}, \{b\}, \{a,b\}, \{a,b,c\}\}$. Let a map $f: X \rightarrow Y$ defined by $f(a)=c, f(b)=a, f(c)=b, f(d)=d$, then f is pgprw continuous map, but not continuous map, as closed set $F=\{c,d\}$ in Y , then

$f^{-1}(F)=\{a,d\}$ in X which is not closed set in X .

Theorem.3.4: If a map $f: (X, \tau) \rightarrow (Y, \sigma)$ is p -continuous map, then it is $pgprw$ -continuous map, but not conversely.

Proof: Follow from the fact that every p -closed set is $pgprw$ closed set [Theorem 2.3].

Example 3.5: Let, $X=Y=\{a,b,c,d\}$, $\tau=\{X, \emptyset, \{a\}, \{b\}, \{a,b\}, \{a,b,c\}\}$ and

$\sigma = \{Y, \emptyset, \{a\}, \{b\}, \{a,b\}, \{a,b,c\}\}$. Let a map $f: X \rightarrow Y$ defined by $f(a)=c, f(b)=a, f(c)=b, f(d)=d$,

Then f is $pgprw$ -continuous map, but not p -continuous map as closed set $F = \{c,d\}$ in Y then $f^{-1}(F)=\{a,d\}$ in X which is not p -closed set in X .

Theorem.3.6: If a map $f: (X, \tau) \rightarrow (Y, \sigma)$ is $pgprw$ -continuous map, then f is gpr -continuous map, but not conversely.

Proof: Follow from the fact that every $pgprw$ -closed set is gpr closed set [Theorem 2.5].

Example 3.7: Let, $X=Y=\{a,b,c\}$, $\tau=\{X, \emptyset, \{a\}, \{b,c\}\}$ and

$\sigma = \{Y, \emptyset, \{a\}\}$. Let a map $f: X \rightarrow Y$ defined by $f(a)=b, f(b)=a, f(c)=c$.

Then f is gpr -continuous map but not $pgprw$ -continuous map as closed set $F = \{b,c\}$ in Y then ; $f^{-1}(F)=\{a,c\}$ in X which is not $pgprw$ -closed set in X .

Theorem.3.8: If a map $f: (X, \tau) \rightarrow (Y, \sigma)$ is $pgprw$ -continuous map, then it is $gspr$ -continuous, but not conversely.

Proof: Follow from the fact that every $pgprw$ -closed set is $gspr$ closed set [Theorem 2.6].

Example 3.9: Let, $X=Y=\{a,b,c\}$, $\tau=\{X, \emptyset, \{a\}, \{b,c\}\}$ and

$\sigma = \{Y, \emptyset, \{a\}\}$. Let a map $f: X \rightarrow Y$ defined by $f(a)=b, f(b)=a, f(c)=c$.

Then f is $gspr$ -continuous map but not $pgprw$ -continuous map as closed set $F = \{b,c\}$ in Y then, $f^{-1}(F)=\{a,c\}$ in X which is not $pgprw$ -closed set in X .

Theorem.3.10: If a map $f: (X, \tau) \rightarrow (Y, \sigma)$ is $pgprw$ -continuous map, then it is gp -continuous map, but not conversely.

Proof: Follow from the fact that every $pgprw$ -closed set is gp closed set [Theorem 2.7].

Example 3.11: Let, $X=Y=\{a,b,c\}$, $\tau=\{X, \emptyset, \{a\}, \{b,c\}\}$ and $\sigma = \{Y, \emptyset, \{a\}\}$. Let a map $f: X \rightarrow Y$ defined by $f(a)=b, f(b)=a, f(c)=c$.

Then f is gp -continuous map but not $pgprw$ -continuous map as closed set $F = \{b,c\}$ in Y , then $f^{-1}(F)=\{a,c\}$ in X which is not $pgprw$ -closed set in X .

Theorem.3.12: Let $f: X \rightarrow Y$ be a map, then the following statements are equivalent

(i) f is $pgprw$ -continuous map

(ii) The inverse image of each open set in Y is $pgprw$ -open in X .

Proof: Assume that $f: X \rightarrow Y$ is $pgprw$ -continuous map, Let G be open in Y , Then G^c is closed in Y . Since f is $pgprw$ -continuous map, $f^{-1}(G^c)$ is $pgprw$ closed in X . But $f^{-1}(G^c) = X - f^{-1}(G)$. Thus $f^{-1}(G)$ is $pgprw$ -open in X .

Conversely, assume that inverse image of each open set in Y is $pgprw$ -open in X . Let F be any closed set in Y , by assumption $f^{-1}(F^c)$ is $pgprw$ -open in X . But $f^{-1}(F^c) = X - f^{-1}(F)$. Thus $X - f^{-1}(F)$ is $pgprw$ -open in X and so $f^{-1}(F)$ is $pgprw$ closed in X . Therefore f is $pgprw$ -continuous map; hence (i) & (ii) are equivalent.

Theorem.3.13: If a map $f: X \rightarrow Y$ is completely continuous map, then it is $pgprw$ -continuous map.

Proof: Suppose that a map $f: (X, \tau) \rightarrow (Y, \sigma)$ is completely continuous map; Let F be closed set in Y then $f^{-1}(F)$ is regular closed in X and $f^{-1}(F)$ is $pgprw$ closed in X . Thus f is $pgprw$ -continuous map.

Remark: The following examples shows that $pgprw$ -continuous maps are independent of β -continuous map, rw -continuous map, rgw -continuous map, $wgr\alpha$ -continuous map, α continuous map, $gprw$ -continuous map, gr -continuous map, R^* -continuous map, rps -continuous map, Semi-continuous map.

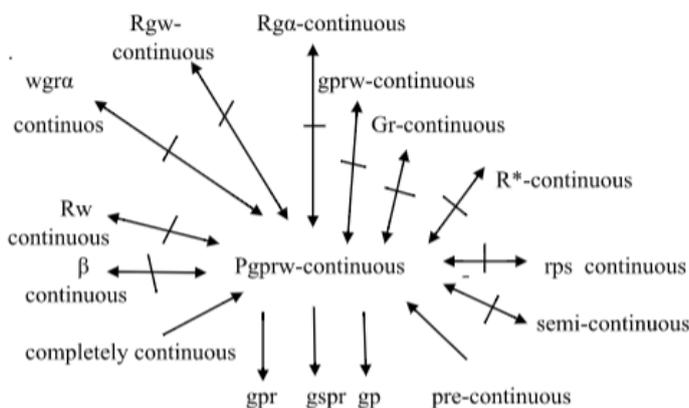
Example 3.14: Let, $X=Y=\{a,b,c\}$, $\tau=\{X, \emptyset, \{a\}, \{b,c\}\}$ and $\sigma = \{Y, \emptyset, \{a\}\}$. Let a map $f: X \rightarrow Y$ defined by $f(a)=b, f(b)=a, f(c)=c$. then f is β -continuous map, rw -continuous map, rgw -continuous map, $wgr\alpha$ -continuous map, $r\alpha$ -continuous map, $gprw$ -continuous map, gr -continuous map, R^* -continuous map, rps -continuous map, Semi-continuous map but f is not $pgprw$ -continuous as closed set $F = \{b,c\}$ in Y then $f^{-1}(F)=\{a,c\}$ in X which is not $pgprw$ -closed set in X .

Example 3.15: Let $X=\{a,b,c,d\}$, $Y=\{a,b,c\}$, $\tau=\{X, \emptyset, \{a\}, \{b\}, \{a,b\}, \{a,b,c\}\}$ and $\sigma = \{Y, \emptyset, \{a\}\}$. Let a map $f: X \rightarrow Y$ defined by $f(a)=b, f(b)=a, f(c)=a, f(d)=c$, Then f is $pgprw$ -continuous map but f is not rw -continuous map, rgw -continuous map, $wgr\alpha$ -continuous map, $rg\alpha$ -continuous map, $gprw$ -continuous map, R^* continuous maps, rps -continuous map respectively as closed set $F = \{b,c\}$ in Y , then $f^{-1}(F)=\{a,d\}$ in X which is not rw -closed, rgw -closed, $wgr\alpha$ -closed, $rg\alpha$ -closed, $gprw$ -closed, R^* -closed, rps closed set in X .

Example 3.16: Let $X=Y=\{a,b,c,d\}$ and $\tau = \{X, \emptyset, \{a\}, \{b\}, \{a,b\}, \{a,b,c\}\}$ and $\sigma = \{Y, \emptyset, \{b,c\}, \{b,c,d\}, \{a,c,d\}\}$. Let map $f: X \rightarrow Y$ defined by $f(a)=c, f(b)=b, f(c)=a, f(d)=d$, then f is $pgprw$ -continuous map but f is not gr -continuous map as closed set $F = \{a\}$ in Y , then $f^{-1}(F)=\{c\}$ in X , which is not gr -closed set in X .

Example 3.17: Let $X=\{a,b,c,d\}$, $Y=\{a,b,c\}$ and $\tau = \{X, \emptyset, \{a\}, \{b\}, \{a,b\}, \{a,b,c\}\}$ $\sigma = \{Y, \emptyset, \{a\}\}$ Let map $f: X \rightarrow Y$ defined by $f(a)=b, f(b)=b, f(c)=a, f(d)=c$, then f is $pgprw$ -continuous map but f is not Semi-continuous map, β -continuous map, sg -continuous maps as closed set $F = \{b,c\}$ in Y then $f^{-1}(F)=\{a,b,d\}$ in X which is not semi-closed, β -closed, sg -closed set in X .

Remark 3.18: From the above discussion and known results we have the following implication



Theorem 3.19: The Composition of two $pgprw$ -continuous maps need not be $pgprw$ -continuous maps and this can be shown by following example.

Example 3.20: Let $X=Y=Z=\{a,b,c\}$ and $\tau = \{X, \emptyset, \{a\}, \{b\}, \{a,b\}, \{a,b,c\}\}$ and $\sigma = \{Y, \emptyset, \{a\}\}$, $\mu = \{Z, \emptyset, \{a\}, \{a,b\}, \{a,c\}\}$ and a maps $f: X \rightarrow Y$, $g: Y \rightarrow Z$ & $g \circ f: X \rightarrow Z$ are identity maps both f & g are $pgprw$ continuous maps but $g \circ f$ not $pgprw$ -continuous map. Since closed set $V = \{b\}$ in Z , $f^{-1}(V)=\{b\}$, which is not $pgprw$ closed set in X .

Theorem 3.21: Let $f: X \rightarrow Y$ is $pgprw$ continuous map function and $g: Y \rightarrow Z$ is continuous map then $g \circ f: X \rightarrow Z$ is $pgprw$ -continuous map.

Proof: Let g be continuous map and V be any open set in Z then $g^{-1}(V)$ is open in Y , Since f is $Pgprw$ -continuous map $f^{-1}(g^{-1}(V))=(g \circ f)^{-1}(V)$ is $pgprw$ -open; hence $g \circ f$ is $pgprw$ -continuous map.

Theorem 3.22: Let $f: X \rightarrow Y$ be a function from a topological space X in to t.s Y .

Iff: $X \rightarrow Y$ is $pgprw$ -continuous map then $f(pgprw-cl(A)) \subseteq cl(f(A))$, for every subset A of X .

Proof: Since $f(A) \subseteq Cl(f(A))$, implies that $A \subseteq f^{-1}(Cl(f(A)))$. Since $Cl(f(A))$ is a closed set in Y and f is $pgprw$ -continuous map then by definition $f^{-1}(Cl(f(A)))$ is a $pgprw$ closed set in X containing A ; hence $pgprw-cl(A) \subseteq f^{-1}(Cl(f(A)))$. Therefore $f(pgprw-cl(A)) \subseteq Cl(f(A))$.

The converse of the above theorem need not be true as seen from the following example

Example 3.23: Let $X=Y=\{a,b,c,d\}$ and $\tau = \{X, \emptyset, \{a\}, \{c,d\}, \{a,c,d\}\}$

and $\sigma = \{Y, \emptyset, \{b,c\}, \{b,c,d\}, \{a,c,d\}\}$. Let map $f: X \rightarrow Y$ defined by $f(a)=d, f(b)=b, f(c)=c, f(d)=d$, for every subset of X , $f(\text{pgprw-cl}(A)) \subseteq \text{cl}(f(A))$, holds ;but f is not pgprw-continuous map. Since closed set $V=\{d\}$ in Y , $f^{-1}(V)=\{a,d\}$ which is not pgprw closed set in X .

Theorem 3.24: Let A be a subset of a topological space X . Then $x \in \text{pgprw-cl}(A)$ if and only if for any pgprw-open set U containing x , $A \cap U \neq \emptyset$.

Proof: Let $x \in \text{pgprw-cl}(A)$ and suppose that, there is a pgprw-open set U in X such that $x \in U$ and $A \cap U = \emptyset$ implies that $A \subset U^c$ which is pgprw-closed in X implies $\text{pgprw-cl}(A) \subseteq \text{pgprw-cl}(U^c) = U^c$. Since $x \in U$ implies that $x \notin U^c$ implies that $x \notin \text{pgprw-cl}(A)$, this is a contradiction. Conversely, Suppose that, for any pgprw-open set U containing x , $A \cap U \neq \emptyset$. To prove that $x \in \text{pgprw-cl}(A)$. Suppose that $x \notin \text{pgprw-cl}(A)$, then there is a pgprw-closed set F in X such that $x \notin F$ and $A \subseteq F$. Since $x \notin F$ implies that $x \in F^c$ which is pgprw-open in X . Since $A \subseteq F$ implies that $A \cap F^c = \emptyset$, this is a contradiction. Thus $x \in \text{pgprw-cl}(A)$.

Theorem 3.25 : Let $f: X \rightarrow Y$ be a function from a topological space X into a topological space Y . Then the following statements are equivalent:

- (i) For each point x in X and each open set V in Y with $f(x) \in V$, there is a pgprw-open set U in X such that $x \in U$ and $f(U) \subseteq V$
- (ii) For each subset A of X , $f(\text{pgprw-cl}(A)) \subseteq \text{cl}(f(A))$.
- (iii) For each subset B of Y , $\text{pgprw-cl}(f^{-1}(B)) \subseteq f^{-1}(\text{cl}(B))$.
- (iv) For each subset B of Y , $f^{-1}(\text{int}(B)) \subseteq \text{pgprw-int}(f^{-1}(B))$.

Proof:(i) \rightarrow (ii) Suppose that (i) holds and let $y \in f(\text{pgprw-cl}(A))$ and let V be any open set of Y . Since $y \in f(\text{pgprw-cl}(A))$ implies that there exists $x \in \text{pgprw-cl}(A)$ such that $f(x) = y$.

Since $f(x) \in V$, then by (i) there exists a pgprw-open set U in X such that $x \in U$ and $f(U) \subseteq V$. Since $x \in \text{pgprw-cl}(A)$, then by theorem 3.24 $U \cap A \neq \emptyset$. $\emptyset \neq f(U \cap A) \subseteq f(U) \cap f(A) \subseteq V \cap f(A)$, then $V \cap f(A) \neq \emptyset$. Therefore we have $y = f(x) \in \text{cl}(f(A))$. Hence $f(\text{pgprw-cl}(A)) \subseteq \text{cl}(f(A))$.

(ii) \rightarrow (i) Let if (ii) holds and let $x \in X$ and V be any open set in Y containing $f(x)$. Let $A = f^{-1}(V^c)$ this implies that $x \notin A$. Since $f(\text{pgprw-cl}(A)) \subseteq \text{cl}(f(A)) \subseteq V^c$ this implies that $\text{pgprw-cl}(A) \subseteq f^{-1}(V^c) = A$. Since $x \notin A$ implies that $x \notin \text{pgprw-cl}(A)$ and by theorem 3.24 there exists a pgprw-open set U containing x such that $U \cap A = \emptyset$, then $U \subseteq A^c$ and hence $f(U) \subseteq f(A^c) \subseteq V$.

(ii) \rightarrow (iii) Suppose that (ii) holds and Let B be any subset of Y . Replacing A by $f^{-1}(B)$ we get from (ii) $f(\text{pgprw-cl}(f^{-1}(B))) \subseteq \text{cl}(f(f^{-1}(B))) \subseteq \text{cl}(B)$. Hence $\text{pgprw-cl}(f^{-1}(B)) \subseteq f^{-1}(\text{cl}(B))$.

(iii) \rightarrow (ii) Suppose that (iii) holds, let $B = f(A)$ where A is a subset of X . Then we get from (iii), $\text{pgprw-cl}(f^{-1}(f(A))) \subseteq f^{-1}(\text{cl}(f(A)))$ implies $\text{pgprw-cl}(A) \subseteq f^{-1}(\text{cl}(f(A)))$.

Therefore $f(\text{pgprw-cl}(A)) \subseteq \text{cl}(f(A))$.

(iii) \rightarrow (iv) Suppose that (iii) holds. Let $B \subseteq Y$, then $Y-B \subseteq Y$. By (iii), $\text{pgprw-cl}(f^{-1}(Y-B)) \subseteq f^{-1}(\text{cl}(Y-B))$ this implies $X-\text{pgprw-int}(f^{-1}(B)) \subseteq X-f^{-1}(\text{int}(B))$.

Therefore $f^{-1}(\text{int}(B)) \subseteq \text{pgprw-int}(f^{-1}(B))$.

(iv) \rightarrow (iii) Suppose that (iv) holds Let $B \subseteq Y$, then $Y-B \subseteq Y$. By (iv), $f^{-1}(\text{int}(Y-B)) \subseteq \text{pgprw-int}(f^{-1}(Y-B))$ this implies that $X-f^{-1}(\text{cl}(B)) \subseteq X-\text{pgprw-cl}(f^{-1}(B))$. Therefore $\text{pgprw-cl}(f^{-1}(B)) \subseteq f^{-1}(\text{cl}(B))$.

Conclusion : In this paper, a new class of maps called Pgprw-Continuous maps are introduced and investigated and we observed that the composition of two pgprw-continuous maps need not be pgprw-continuous maps. in future the same process will be analyzed for pgprw-properties.

References:

- [1]. N .Levine, Semi-open sets and semi-continuity in topological spaces,70(1963), 36- 41.
- [2]. Precious Jane Fiesta Lapura & Helen moso Rava ,Some forms of rgw-continuous function,intjournal of math analysis,Vol.8,2014,no.30,1457-1463.
- [3]. R.S.Wali, on some topics in general and fuzzy topological spaces ph.d thesis K.U.Dharwad (2007).
- [4]. M. E. Abd El-Monsef, S.N. El-Deeb and R.A.Mahmoud, β -open sets and β -continuous mappings, Bull. Fac. Sci. Assiut Univ., 12(1983), 77-90.
- [5]. A. Jayalakshmi & C.Janaki, on ω gr α -continuous functions in Topological Spaces,int j of maths 3(6)2012;2386-2392.
- [6]. A.Vadivel & K.vairamamanickam,rg α -continuous Maps and Some oftheir Properties, Acta Ciencia Indica, (in press).
- [7]. V.Joshi,S.Gupta,N.Bhardwaj,R,kumar, on Generalised pre Regular weakly(gprw)-closed functions in Topological Spaces,pure mathematical science,vol.2 2013,no.1,13-21;Hikari Ltd.
- [8]. M.Yoshimura,T.Miwa & T.Noiri; a gr-closed functions and g-closed functions in topological spaces ;Dept of Mathematics,faculty of science, Shimane university,japan (1993).
- [9]. C.Janaki & Renu Thomas , on R*- Closed sets in Topological Spaces, Int J of Math Archive 3(8) 2012, 3067-3074 .
- [10]. T. Shlya Isac Mary & P.Thangavelv, on rps-continuous and rps-irresolute functions,IJMA 2(1) (2011),159-162.
- [11]. A.S.Mashhour, M.E.Abd El-Monsef and S.N.El-Deeb, On pre-continuous and weak pre continuous mappings, Proc. Math. Phys. Soc. Egypt, 53(1982), 47-53.
- [12]. I.Arockiarani, k.Balachandran and J.dontchev,some characterization of gp-irresolute and gp-continuous maps between topological spaces,mem.fac.kochi univ ser A math.,20(1999),93-104.
- [13]. Govindappa Navalagi, Chandrashakarappa A.S. & S.V.Gurushantanavar, Int.Jour of Mathematical sciences, Vol.2 no.1 jan 2012,pp-231-237,gspr functions in topological spaces.
- [14]. Y. Gnanambal and K.Balachandran,on gpr-continuous functions in topological spaces;indian J.pure appl math 30(6);581-593 june 1999.
- [15]. P.Sundaram,H.Maki, & K.Balachandran,sg- continuous maps and semi- $T_{1/2}$ Spaces Bull.Fukoka.uni.ed part III,40(1991),33-40.
- [16]. S.P.Arya and R.Gupta,On strongly continuous maps,Kyungpook Math.J.14:131:143,1974.
- [17]. R.S.Wali And Vivekananda Dembre ;On Pre Generalized Pre Regular Weakly Closed Sets in Topological Spaces ;Journal of Computer and Mathematical Sciences, Vol.6(2),113-125, February 2015.
- [18]. R.S.Wali And Vivekananda Dembre;On Pre Generalized Pre Regular Weakly Open Sets and Pre Generalized Pre Regular Weakly Neighbourhoods inTopological Spaces, Annals of Pure and Applied MathematicsVol. 10, No.1, 2015;Published on 12 April 2015.
- [19]. R.S.Wali And Vivekananda Dembre;On pre generalized pre regular weakly interior and pre generalized pre regular weakly closure in topological spaces; international research journal of pure algebra Feb 2016(in press).
- [20]. M.Stone , Application of the theorey of Boolean rings to general topology,trans amer math soc 41,374-481(1937).